

# Fractional Base Station Cooperation Cellular Network

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# Contents

- **Background**
  - Cell-edge problem
  - Conventional solution for the cell-edge problem
  - Base station cooperation
- **Base station cooperation block diagonalization multi-user MIMO**
  - Combination of multi-user
  - Cooperative region
- **Fractional base station cooperation cellular network**
  - Fractional Base Station Cooperation
  - Dynamic clustering
- **Numerical simulation**
- **Conclusion**

# Cell-edge problem

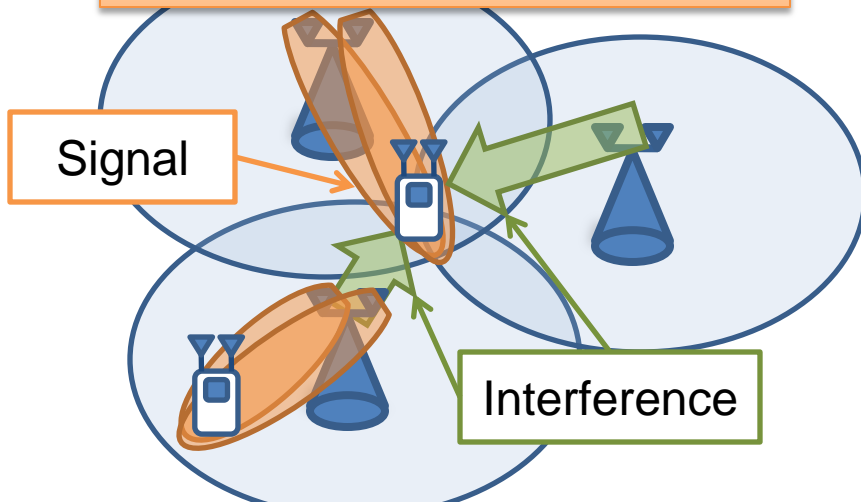
- **If user at the cell-edge location**

- Low SNR
- Co-channel interference from adjacent BSs
- High antenna correlation

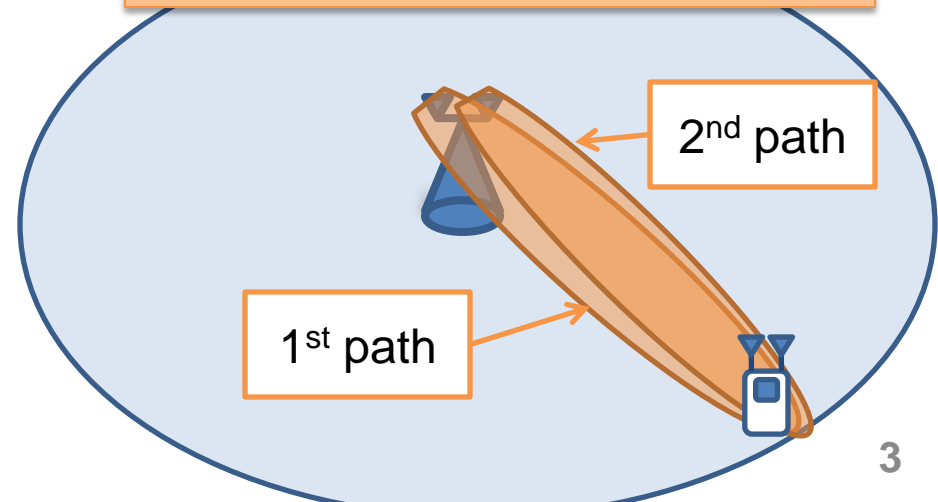
➔ **Low user throughput**

➔ **Cell-edge problem**

Co-channel interference



High antenna correlation



# Conventional solution for cell-edge problem

- **Conventional solution**

- Frequency reuse

- Each BSs uses different frequency channel from surrounding cells.
- ✘ It causes degrading of system throughput.

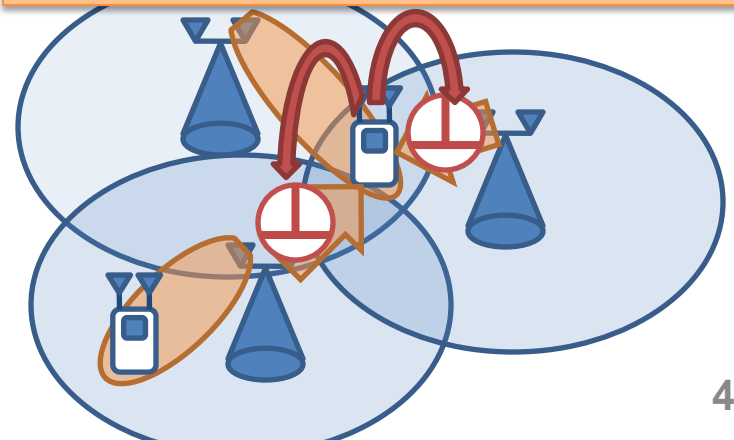
- Interference cancellation using terminal adaptive array

- cancels interference by terminals.
- ✘ It requires many antennas to perform multiplexing and cancellation at the same time.

Frequency reuse



Interference cancellation using terminal adaptive array



# Base station cooperation

- **Base Station Cooperation (BSC)**

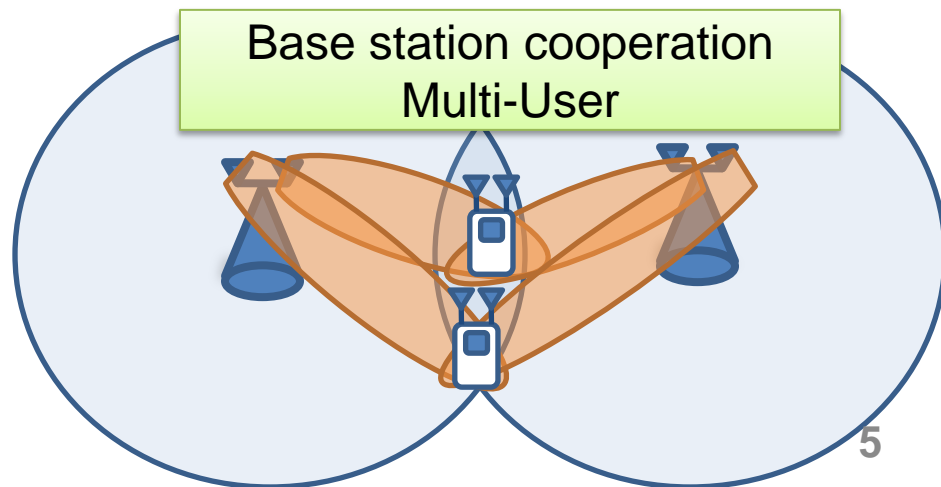
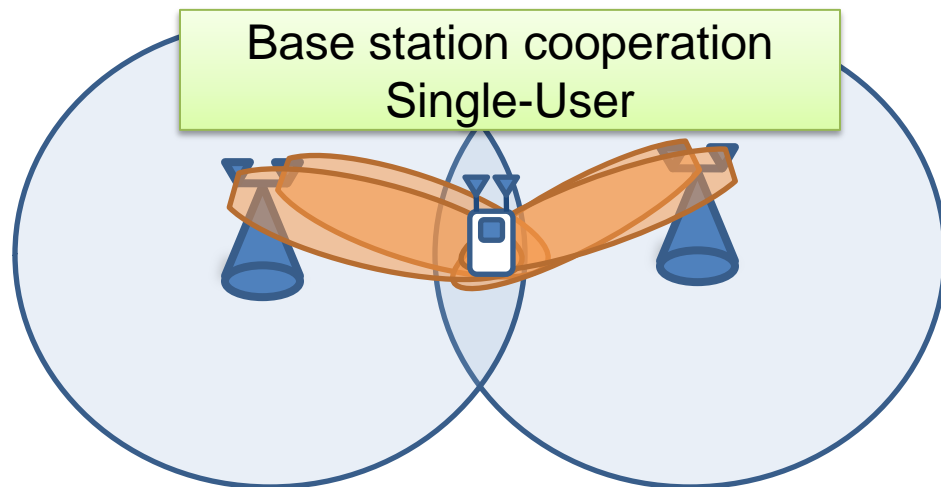
- BSC transmits multiple streams to cooperate with adjacent BSs.
- There are no problems of nor inter-cell interference nor high antenna correlation.

- **BSC single-user (BSC-SU)**

- For single user
- ✗ BSC-SU wastes many resources to a user.

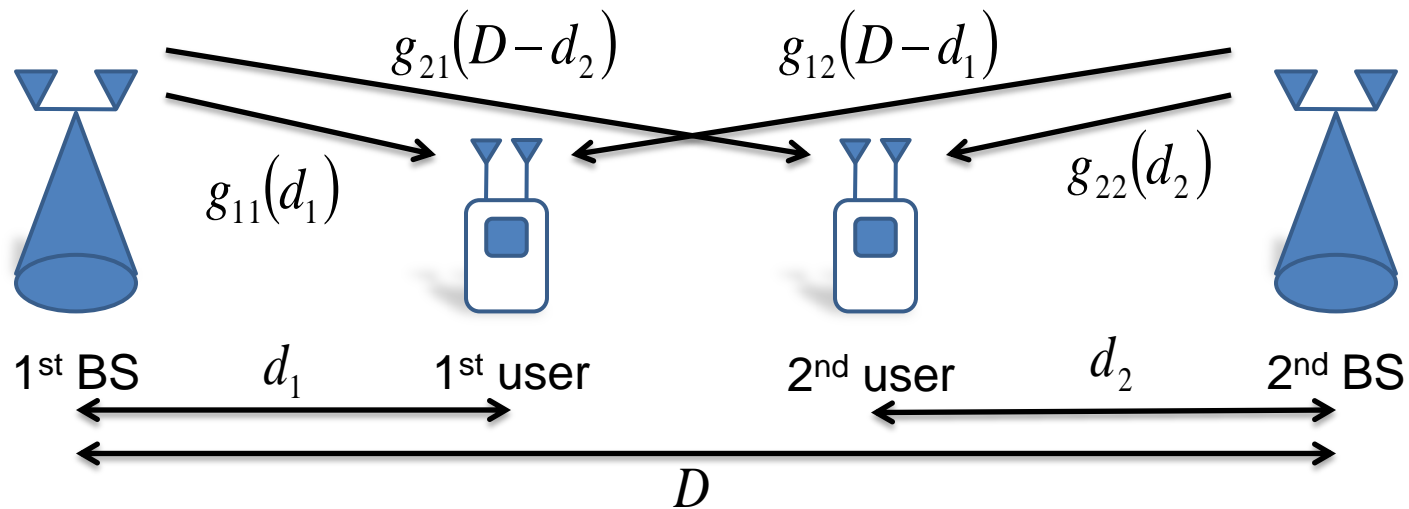
- **BSC multi-user (BSC-MU)**

- For multiple users
- ✓ BSC-MU uses resource more efficient than BSC-SU.



# Base station cooperation block diagonalization multi-user MIMO

- Transmission model of  $(K_{BS}, M) \times (K_{MS}, N)$  BSC-MU-MIMO



$d_i$  : distance between  $i$ th BS and  $i$ th user       $g_{ij}$  : pathloss between  $j$ th BS and  $i$ th user

- Receive signal of  $i$ th user

$$\mathbf{y}_i = \mathbf{H}_{i1} \mathbf{x}_{i1} + \mathbf{H}_{i2} \mathbf{x}_{i2} + \cdots + \mathbf{H}_{iK_{BS}} \mathbf{x}_{iK_{BS}} + \mathbf{n}_i = \mathbf{H}_i \mathbf{Q}_i \tilde{\mathbf{V}}_i \mathbf{s}_i + \mathbf{n}_i$$

$\mathbf{y}_i$  : receive signal vector

$\mathbf{H}_{ij}$  : channel matrix

$\mathbf{Q}_i$  : precoding matrix of block diagonalization

$\mathbf{x}_{ij}$  : transmit signal vector

$\mathbf{n}_i$  : noise vector

$\tilde{\mathbf{V}}_i$  : precoding matrix of SVD-MIMO

$\mathbf{s}_i$  : transmit data signal vector

# Base station cooperation block diagonalization multi-user MIMO

- Precoding matrix  $\mathbf{Q}$

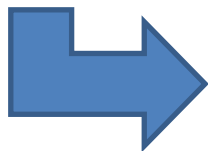
$$\left[ \mathbf{H}_1^T, \dots, \mathbf{H}_{i-1}^T, \mathbf{H}_{i+1}^T, \dots, \mathbf{H}_{K_{MS}}^T \right]^T = \mathbf{H}_{\setminus i} \quad \text{svd}(\mathbf{H}_{\setminus i}) = \mathbf{U} \begin{bmatrix} \Sigma & \mathbf{O} \end{bmatrix} \begin{bmatrix} \mathbf{V}_{\setminus i}^H & \mathbf{Q}_i \end{bmatrix}^H$$

- Block diagonalization

$$\begin{bmatrix} \mathbf{y}_1 \\ \vdots \\ \mathbf{y}_{K_{MS}} \end{bmatrix} = \begin{bmatrix} \mathbf{H}_1 \mathbf{Q}_1 \tilde{\mathbf{V}}_1 & \cdots & \mathbf{H}_1 \mathbf{Q}_{K_{BS}} \tilde{\mathbf{V}}_{K_{BS}} \\ \vdots & \ddots & \vdots \\ \mathbf{H}_{K_{MS}} \mathbf{Q}_1 \tilde{\mathbf{V}}_1 & \cdots & \mathbf{H}_{K_{MS}} \mathbf{Q}_{K_{BS}} \tilde{\mathbf{V}}_{K_{BS}} \end{bmatrix} \begin{bmatrix} \mathbf{s}_1 \\ \vdots \\ \mathbf{s}_{K_{BS}} \end{bmatrix} + \begin{bmatrix} \mathbf{n}_1 \\ \vdots \\ \mathbf{n}_{K_{MS}} \end{bmatrix}$$

$$= \begin{bmatrix} \tilde{\mathbf{H}}_1 \tilde{\mathbf{V}}_1 & \cdots & \mathbf{O} \\ \vdots & \ddots & \vdots \\ \mathbf{O} & \cdots & \tilde{\mathbf{H}}_{K_{MS}} \tilde{\mathbf{V}}_{K_{BS}} \end{bmatrix} \begin{bmatrix} \mathbf{s}_1 \\ \vdots \\ \mathbf{s}_{K_{BS}} \end{bmatrix} + \begin{bmatrix} \mathbf{n}_1 \\ \vdots \\ \mathbf{n}_{K_{MS}} \end{bmatrix}$$

$$\mathbf{H}_j \mathbf{Q}_i = \begin{cases} \tilde{\mathbf{H}}_i & (j = i) \\ \mathbf{O} & (j \neq i) \end{cases}$$



**Channel matrix is block diagonalized**

# Base station cooperation block diagonalization multi-user MIMO

- We decompose the channel matrix into fading matrix and pathloss matrix

$$\mathbf{H}_i = [\mathbf{H}_{i1} \quad \mathbf{H}_{i2}] = [\mathbf{H}_{i1}^{\text{iid}} \quad \mathbf{H}_{i2}^{\text{iid}}] \begin{bmatrix} \mathbf{G}_{i1} & \mathbf{O} \\ \mathbf{O} & \mathbf{G}_{i2} \end{bmatrix} = \mathbf{H}_i^{\text{iid}} \mathbf{G}_i \quad \mathbf{H}_{ij}^{\text{iid}} : \text{fading matrix} \\ \mathbf{G}_{ij} = \sqrt{g_{ij}} \mathbf{I}$$

- Block diagonalization precoding matrix of BSC

$$\mathbf{Q}_i = \mathbf{H}_{j \neq i}^\perp = \frac{1}{\|\mathbf{G}_{j \neq i}^{-1}\|_F} \mathbf{G}_{j \neq i}^{-1} (\mathbf{H}_{j \neq i}^{\text{iid}})^\perp \quad \mathbf{H}_{j \neq i}^{\text{iid}} (\mathbf{H}_{j \neq i}^{\text{iid}})^\perp = \mathbf{O} \Rightarrow \mathbf{H}_i \mathbf{Q}_{j \neq i} = \mathbf{O}$$

- Receive signal of  $i$ th user

$$\mathbf{y}_i = \mathbf{H}_i \mathbf{Q}_i \tilde{\mathbf{V}}_i \mathbf{s}_i + \mathbf{n}_i = \tilde{\mathbf{H}}_i \tilde{\mathbf{V}}_i \mathbf{s}_i + \mathbf{n}_i$$

$$\tilde{\mathbf{H}}_i = \mathbf{H}_i \mathbf{Q}_i = \frac{1}{\|\mathbf{G}_{j \neq i}^{-1}\|_F} \mathbf{H}_i^{\text{iid}} \mathbf{G}_i \mathbf{G}_{j \neq i}^{-1} (\mathbf{H}_{j \neq i}^{\text{iid}})^\perp = \sqrt{\frac{g_{11}g_{22} + g_{12}g_{21}}{g_{j \neq i1} + g_{j \neq i2}}} \tilde{\mathbf{H}}_i^{\text{iid}}$$

$\tilde{\mathbf{H}}_i^{\text{iid}}$  : The equivalent fading matrix of  $i$ th user



# Base station cooperation block diagonalization multi-user MIMO

- **Transmit power from  $j$ th BS**

$$P_j = E[\mathbf{x}_j^H \mathbf{x}_j] \leq \Omega P$$

- **Power normalization factor**

–  $\Omega$  regulates the transmit power

$$\Omega = \begin{cases} \frac{1}{\frac{g_{12}}{g_{11} + g_{12}} + \frac{g_{22}}{g_{21} + g_{22}}} & d_1 \geq d_2 \\ \frac{1}{\frac{g_{11}}{g_{11} + g_{12}} + \frac{g_{21}}{g_{21} + g_{22}}} & d_1 \leq d_2 \end{cases}$$

$\Omega$  : power normalization factor

$P$  : maximum BS transmit power

$$\mathbf{x}_j = [\mathbf{x}_{1j}, \dots, \mathbf{x}_{K_{MS}j}]$$

: transmit signal of  $j$ th BS

- **Average receive SNR of  $i$ th user**

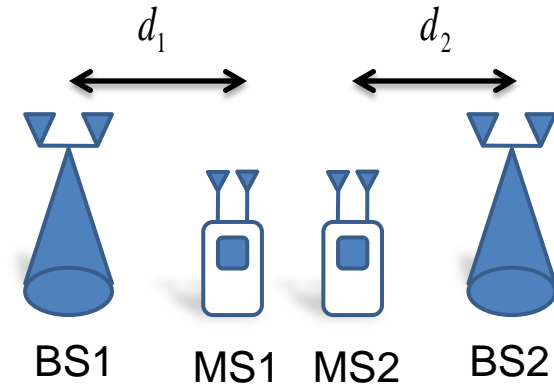
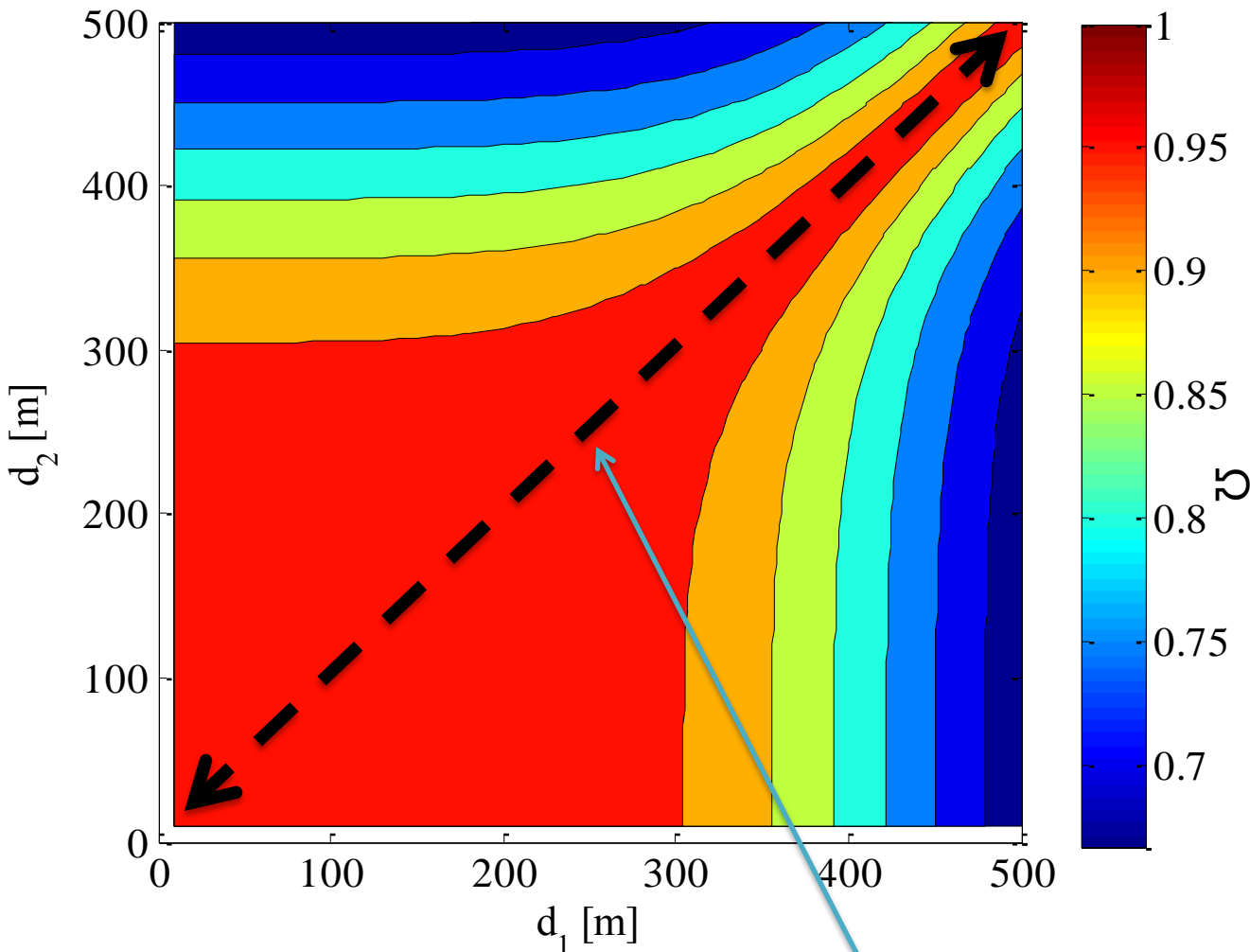
$$\gamma_i = \frac{E\left[|\tilde{\mathbf{H}}_i \tilde{\mathbf{V}}_i s_i|^2\right]}{M\sigma^2} = \frac{g_{11}g_{22} + g_{12}g_{21}}{g_{j \neq i1} + g_{j \neq i2}} \frac{\Omega P}{\sigma^2}$$

- **Capacity of  $i$ th user**

$$C_i = \sum_{k=1}^2 \log_2(1 + \lambda_k \gamma_i)$$

$\lambda_k$  :  $k$ th eigenvalue of equivalent channel

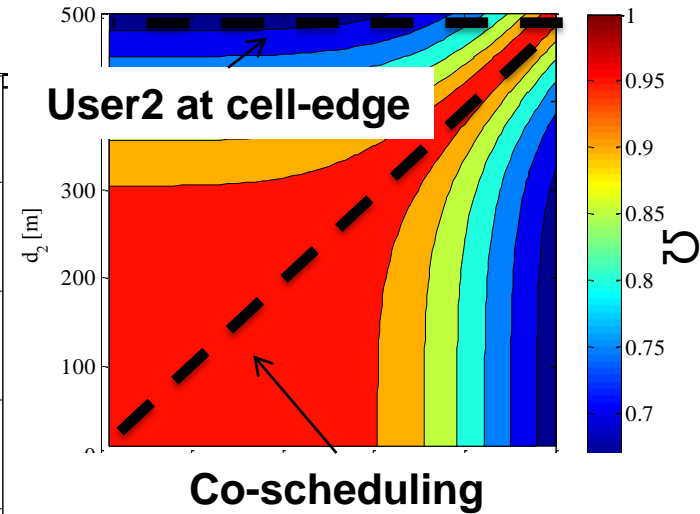
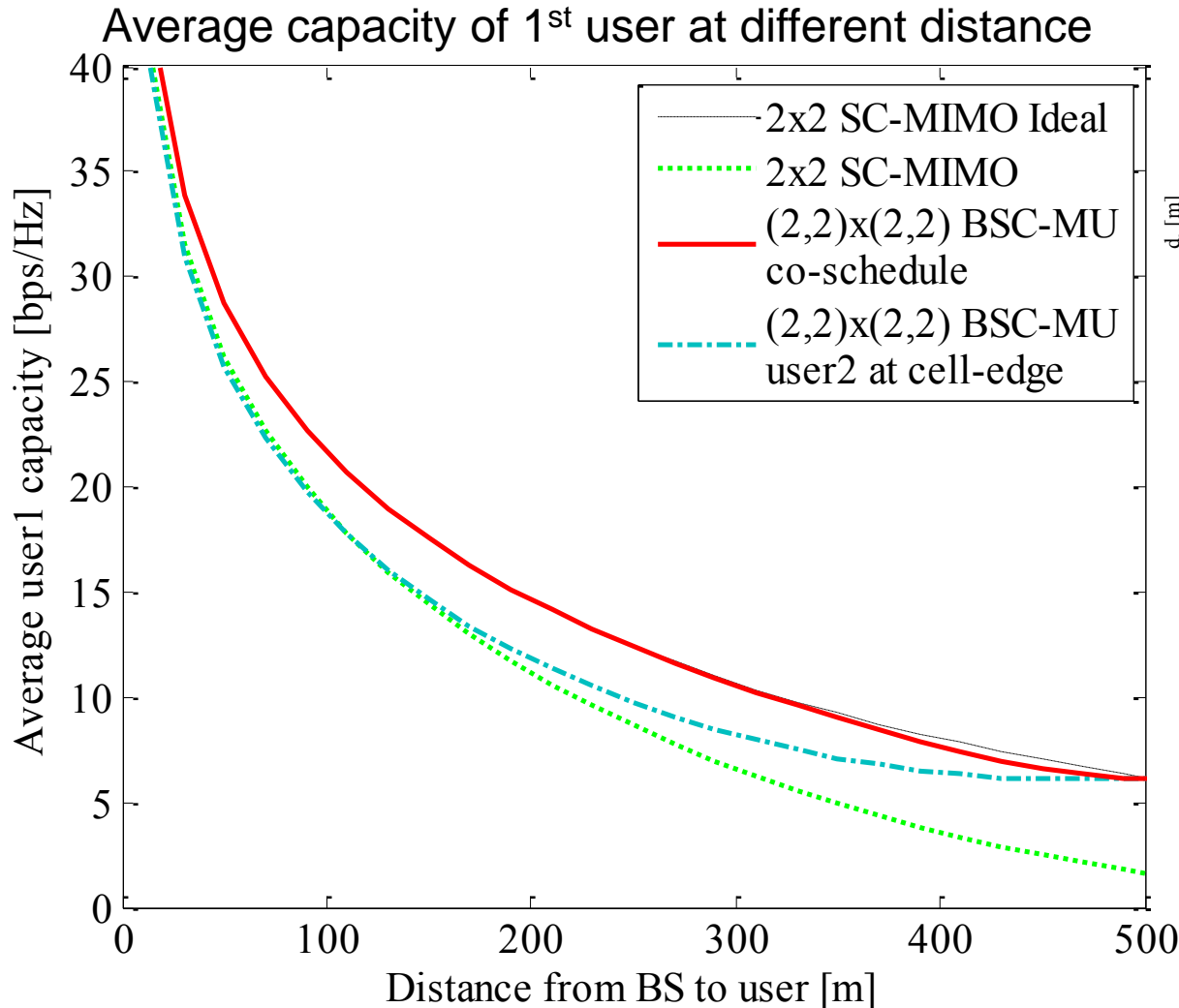
# Power normalization factor $\Omega$



- $d_1 = d_2$   
 $\Omega_{\max} = 1$
- $d_1 \gg d_2, d_1 \ll d_2$   
 $\Omega_{\min} = 2/3$

**Co-scheduling**  
The BSs select users with the same SINR

# Capacity of (2,2)x(2,2) BSC-MU-MIMO



- **Co-scheduling**  
BSC-MU is almost the same capacity as 2x2 SC-MIMO ideal
- **User2 at cell-edge**  
Capacity is decreased about 3bps where distance is from 100m to 300m



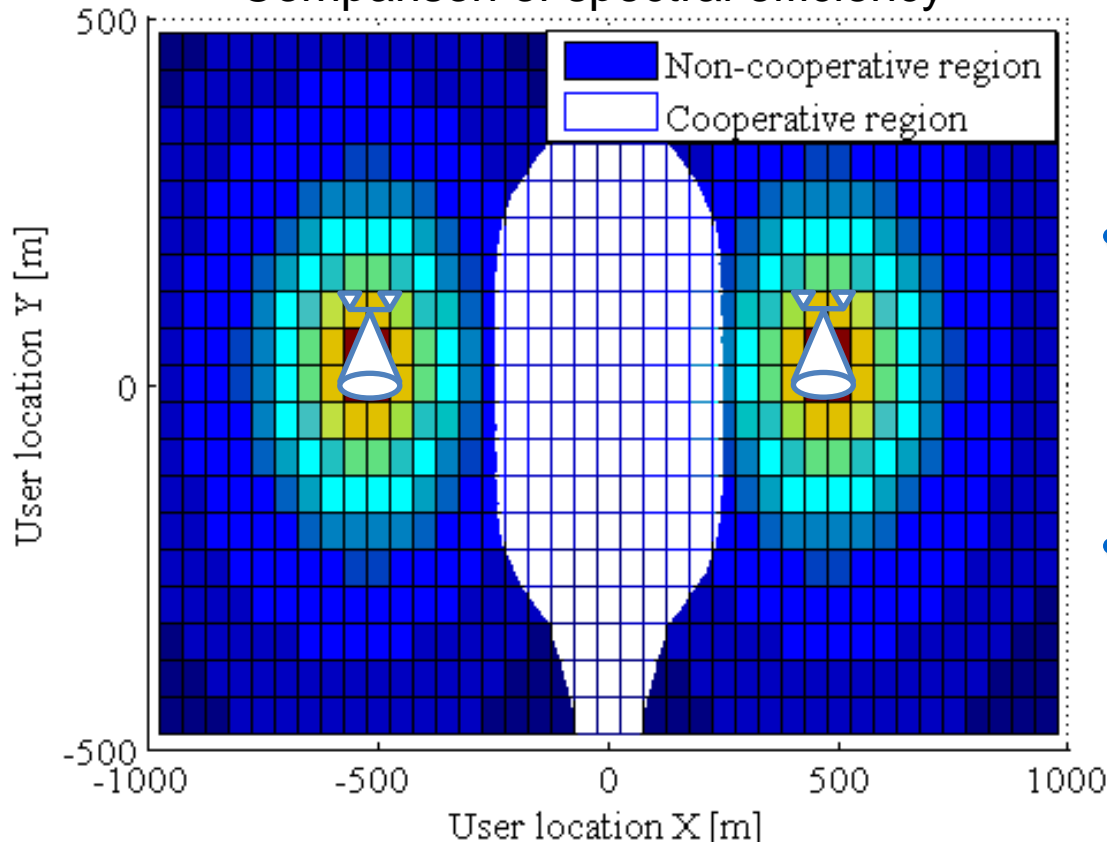
**Co-scheduling is the optimal user selection**

# Cooperative region

- **Analysis considering overhead is necessary**

- Overhead : the cost of resource for transmission (ex. Reference signal, guard band, cyclic prefix)

Comparison of spectral efficiency



- **Spectral efficiency**

$$R^{\text{SC}} = \chi_{\text{SU}} C^{\text{SC}}$$

$$R^{\text{MC}} = \chi_{\text{MU}} C^{\text{MC}}$$

$\chi$  : bandwidth inefficiencies considering overhead

- **Cell-inner**

- Non-cooperative region
  - Single-cell MIMO is efficient at cell-inner

- **Cell-edge**

- Cooperative region
  - BSC MIMO is efficient at cell-edge

# Fractional Base Station Cooperation

- **Single-cell MIMO** (conventional cellular system)
  - Cell-inner : efficient
  - Cell-edge : not efficient
- **Base station cooperation MIMO**
  - Cell-inner : not efficient
  - Cell-edge : efficient



## Fractional Base Station Cooperation (FBSC)

- Cell-inner : uses single-cell MIMO
- Cell-edge : uses BSC MIMO

FBSC is performed to achieve gains both at the cell-inner and cell-edge.

# Cooperation clustering

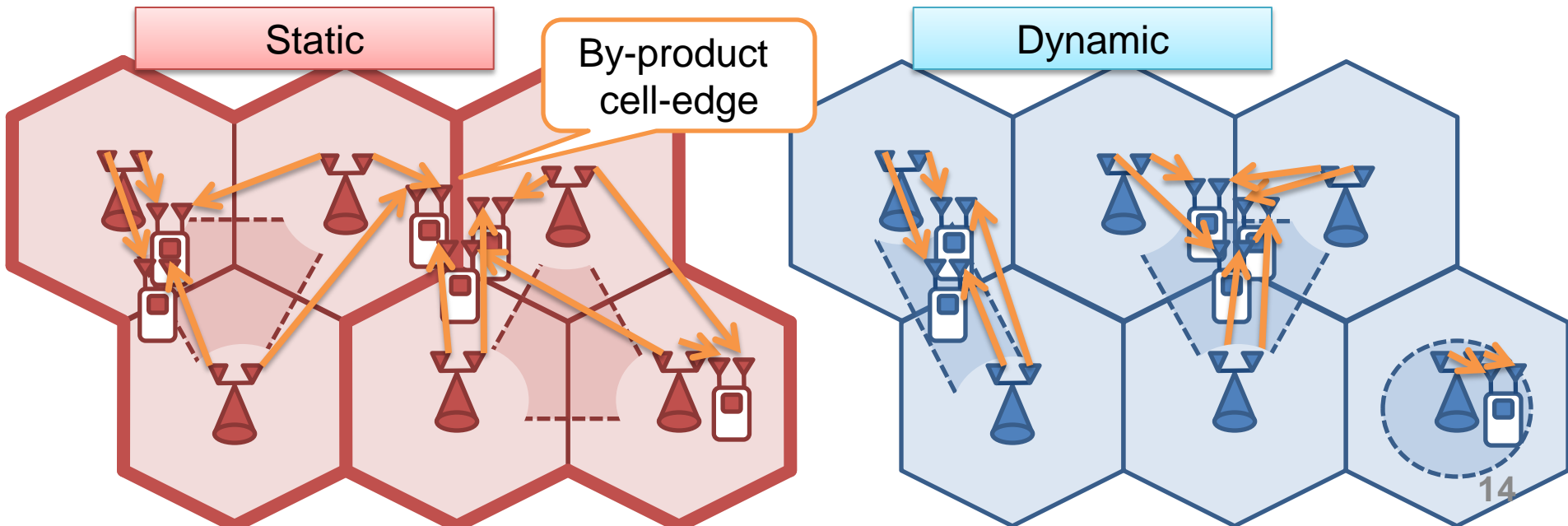
- Clustering

- Static clustering

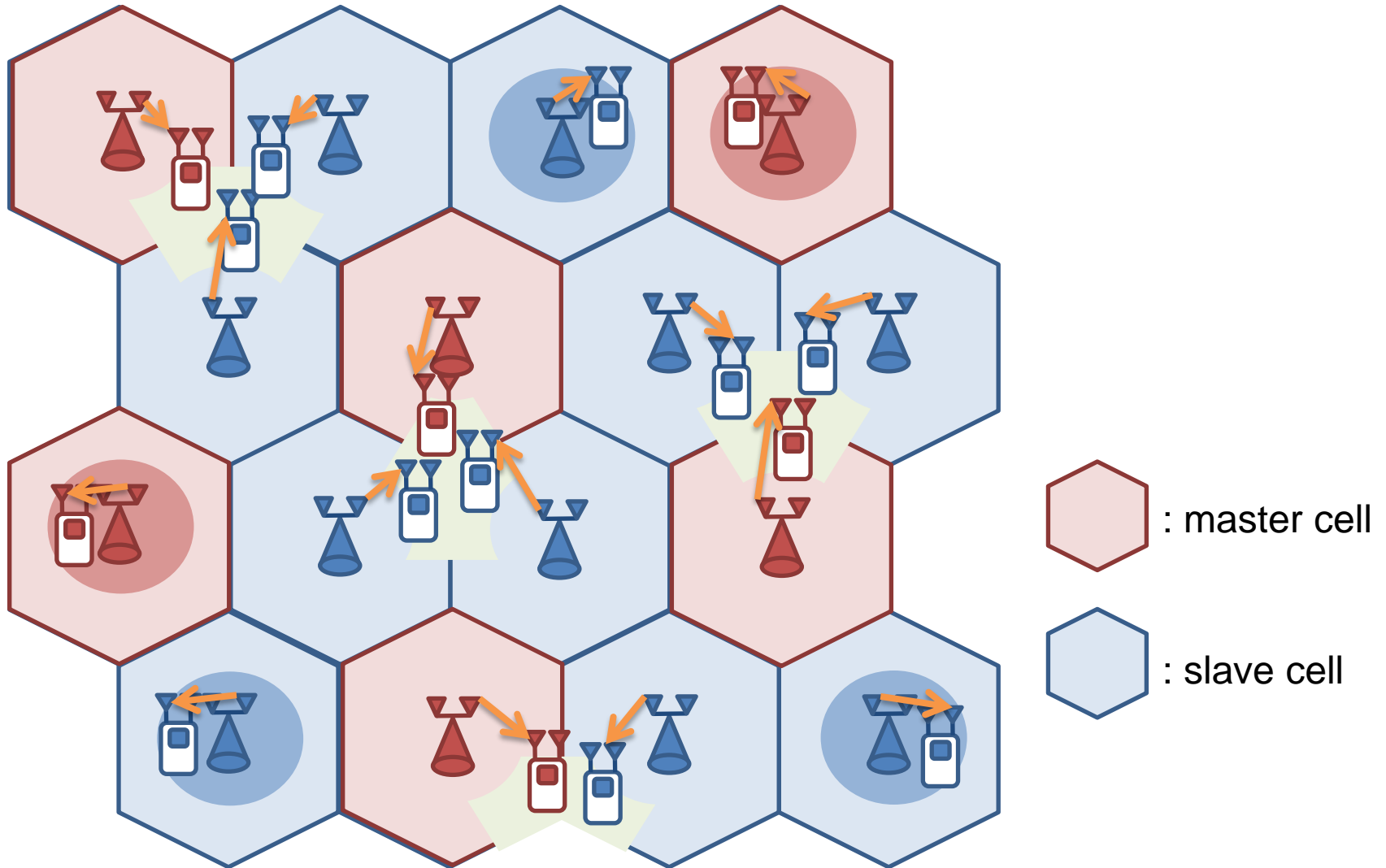
- Cooperation set is fixed
    - ✗ By-product cell-edge is created.

- Dynamic clustering

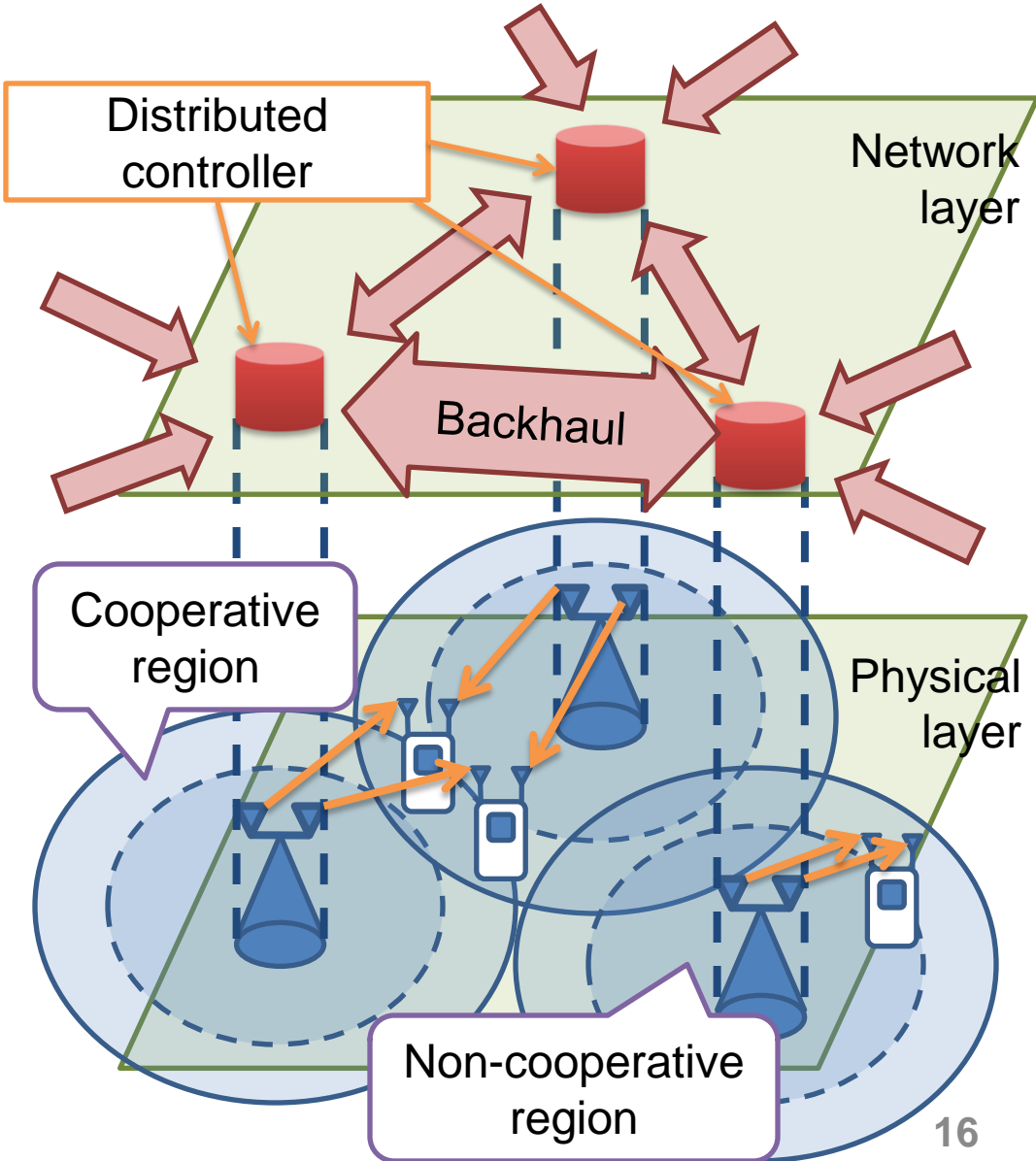
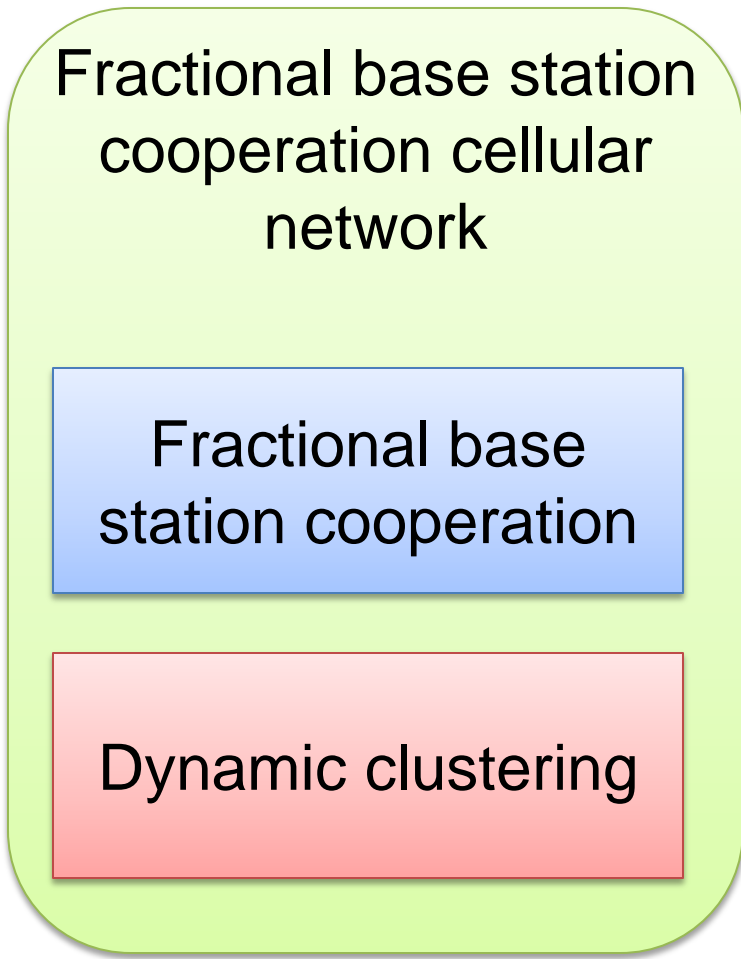
- makes cooperation set adaptively.
    - ✓ Cooperation is efficient at all cell-edges.



# Dynamic clustering



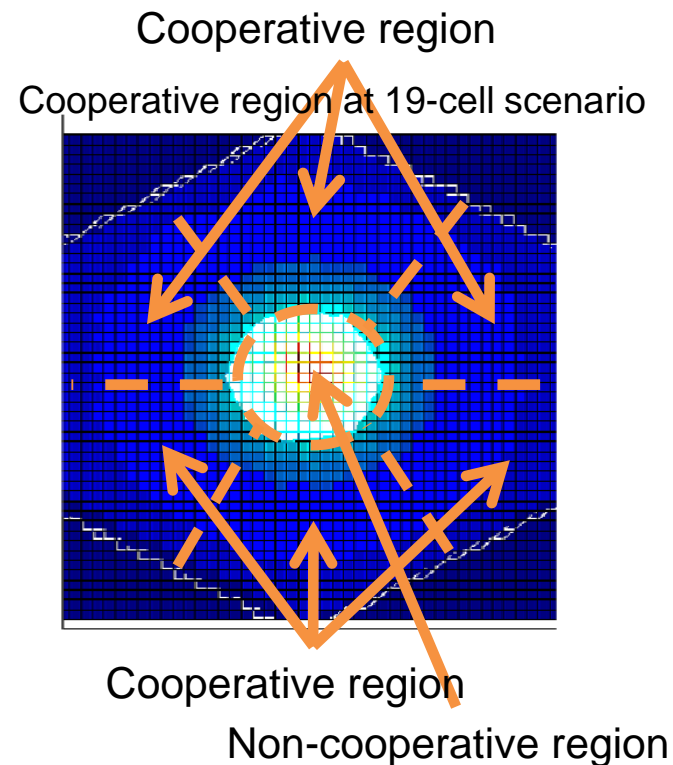
# Fractional base station cooperation cellular network





# Simulation scenario

- **Comparison transmission**
  - Single-cell SISO
  - Single-cell MIMO
    - 2x2 SVD-MIMO
  - Multi-cell static clustering
    - BSC is performed at all locations
    - Static clustering
  - Fractional Base Station Cooperation Cellular Network (FBSC-CN)



# Simulation scenario

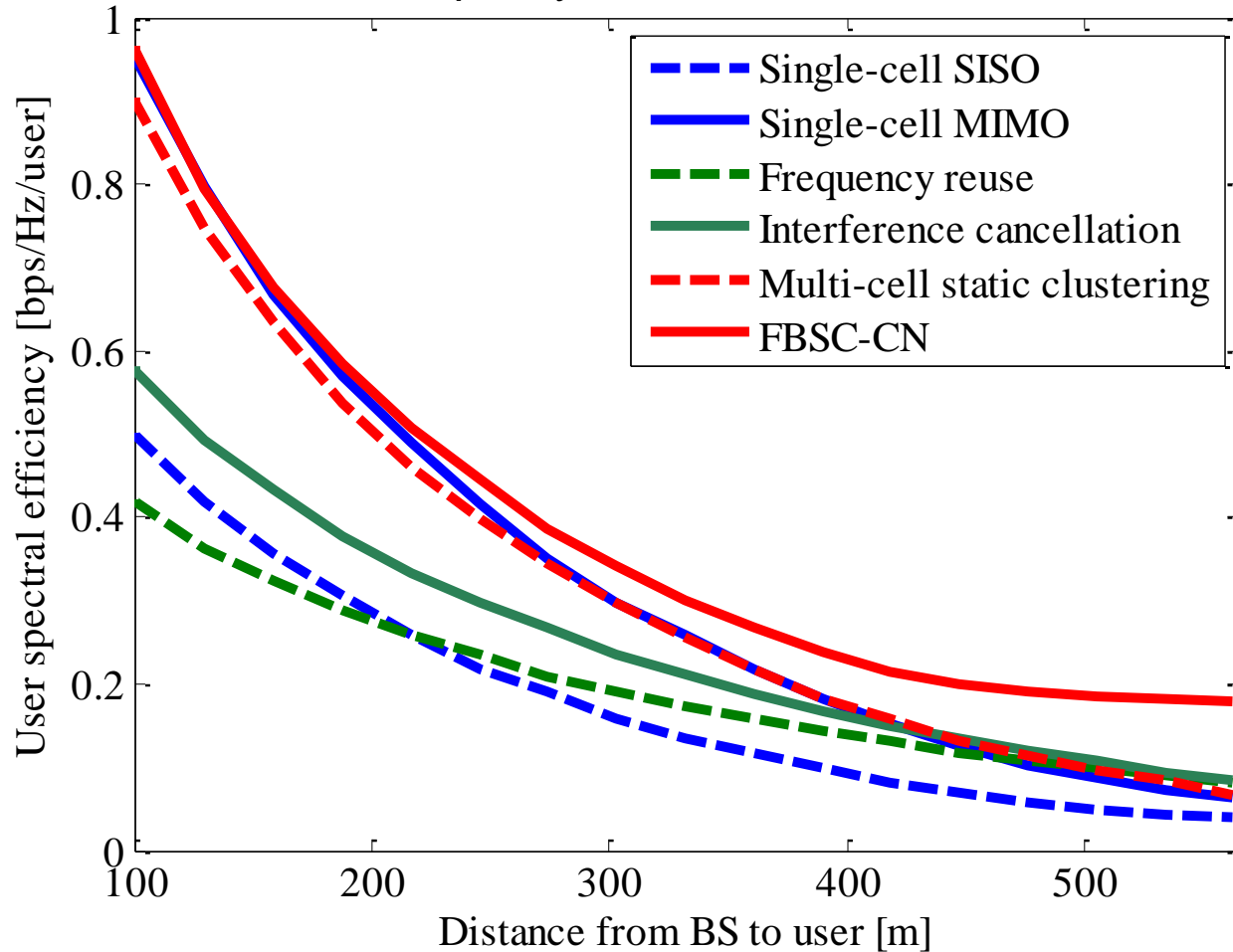
## Simulation parameter

Parameters	Values
Number of cell	19 cells
Number of user	10 users / cell
Number of cooperation set	3 cells
Number of antenna ( BS, user )	1, 1 (SISO) or 2, 2 (MIMO)
Channel model	i.i.d. Rayleigh
Pathloss model	$34.5 + 35\log_{10}(d[m])$ [dB] (3GPP TR 25.996 : Urban Macro)
Transmit power	40[dBm]
Noise level	-100[dBm]
Site to site distance	1000 m
Scheduler	Round-robin & co-scheduling
Single-user MIMO scheme	SVD-MIMO
Multi-user MIMO scheme	Generalized BD [*]

\* V. Stankovic, M. Haardt, "Generalized design of multi-user MIMO precoding matrices," *IEEE Trans. Wireless Commun.*, vol.7, no.3, pp.953-961, Mar. 2008.

# Simulation result

User capacity at the distance locations

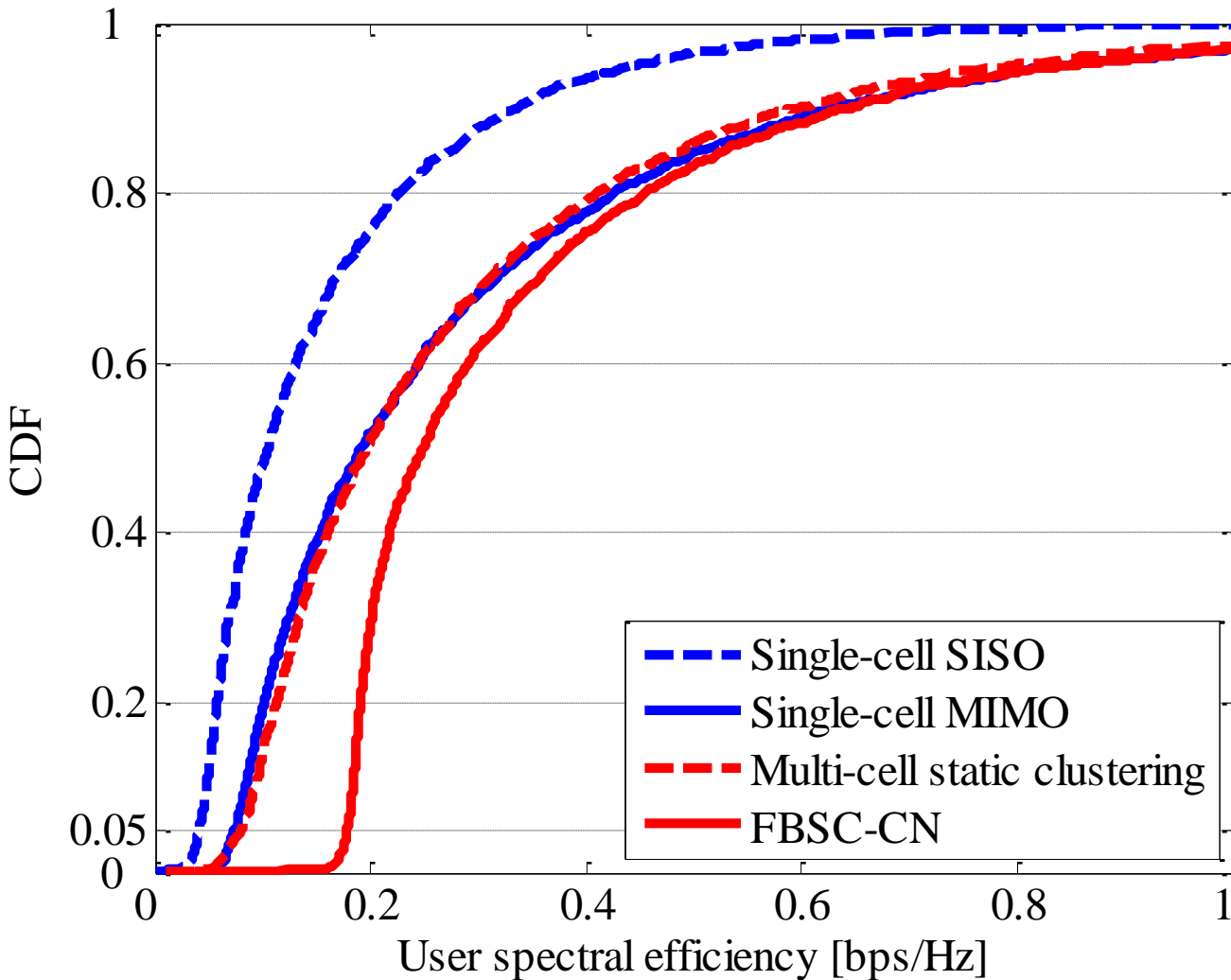


## Fractional BSC

- User capacity at the cell-inner is as high as Single-cell MIMO
- User capacity at the cell-edge is almost the same with BS cooperation

# Simulation result

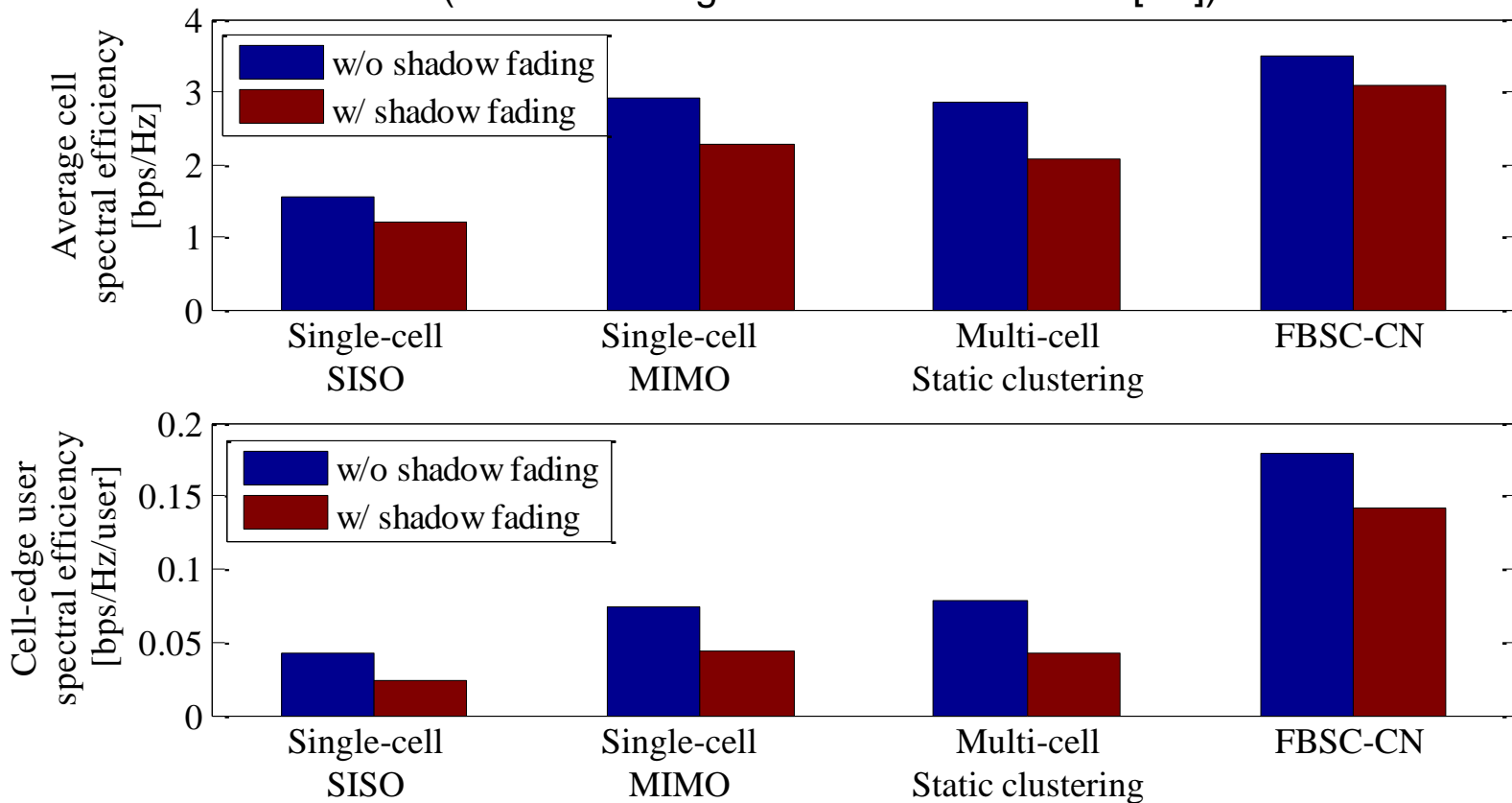
CDF of instantaneous capacity at cell-edge user



- FBSC is higher capacity than other scheme at all probability

# Simulation result

Average cell spectral efficiency and cell-edge spectral efficiency  
(shadow fading standard deviation = 8[dB])



- The average cell spectral efficiency of FBSC is slightly improved than single-cell MIMO
- The cell-edge user spectral efficiency of FBSC is 2.4 times as high as that of single-cell MIMO

# Conclusion

- **BSC solves the cell-edge problem.**
- **Fractional BSC is proposed.**
  - FBSC performs to achieve gains both at the cell-inner and cell-edge.
- **FBSC cellular network is proposed.**
  - In FBSC-CN, cooperation sets are constructed dynamically.
- **Numerical simulation shows that FBSC performs efficiently both at cell-inner and cell-edge.**

**Thank you for your attention.**