

Polarization behavior of Polarized MIMO System

Measurement, Modeling and Statistical Validation

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Outline

I. Motivation

- MIMO: Benefits and Issues
- Objective of This Study

II. Previous Work

- Measurement and Parameter estimation
- Regression analysis of polarization behavior

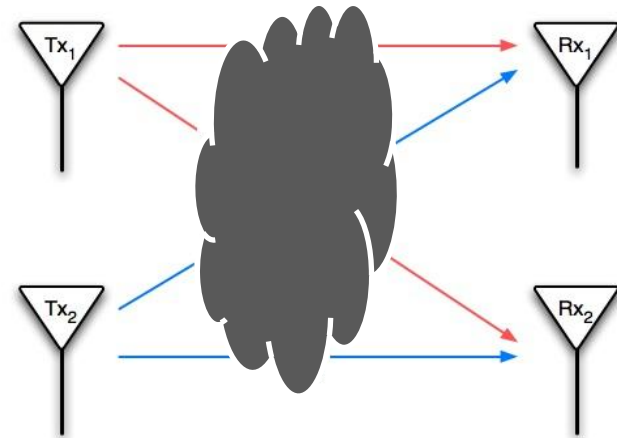
III. Main Results

- Procedure of Hypothesis Testing
- Results

IV. Conclusions

Benefits of MIMO

- MIMO:
Multiple antennas at both Tx and Rx
- Benefits
 - Higher spectral efficiency
 - Higher throughput
 - Higher reliability



Pre-Condition: **Multipath rich environment**

⇒ Receiver can separate the data stream

- “The benefits” heavily depends on the **propagation channel**
“Channel” is a main factor which we can not control.

Issues of MIMO

In the real world

- Inadequate scattering environment = Ricean fading
- Inadequate antenna spacing = Data stream correlation

- “MIMO” discovered new dimension = **Space**
..but Space is also finite.
- New dimension again: **Polarization**
 - Orthogonal by nature (V and H)
 - At least two data streams even in the severe environment
 - Realize compact antenna system



MIMO Wireless Router
(D-Link Systems Inc.)

Polarization diversity

is essential for MIMO (Spatial diversity) system

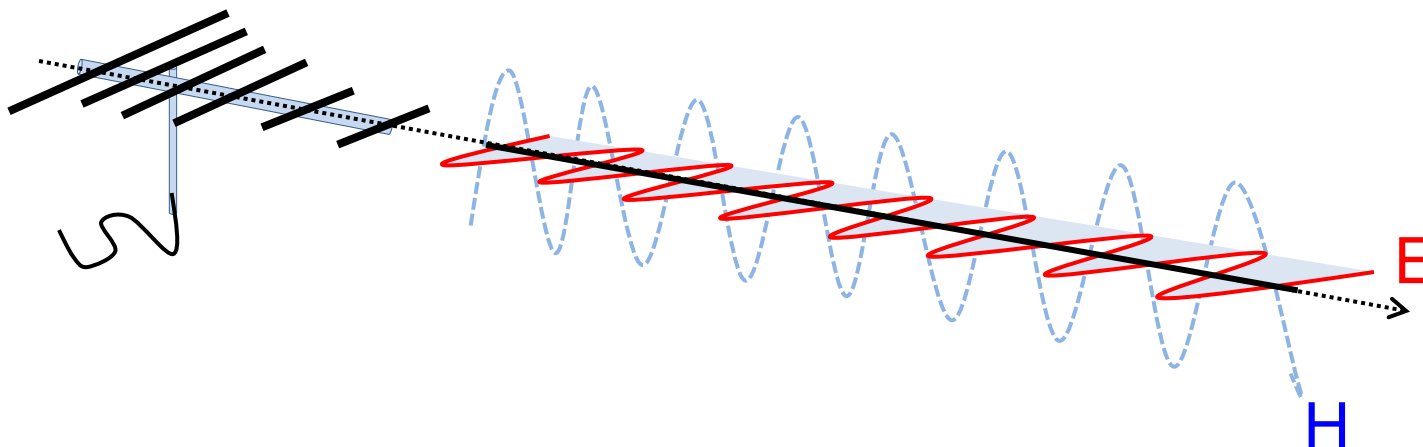
Objective

Quantifying the degree of depolarization to compare different measurement data in a strictly same sense.

- Establishment of good channel model is essential for the all aspects of radio system design
 - Antenna, Signal processing algorithm and Modulation/coding technique
- What kind of factors are insufficient in the current channel model?
 - Investigation of temporal behavior caused by moving scatterers
 - Including diffuse scattering in the model
 - Consideration of spherical mode expansion (solving plan wave limitation)
 - **Polarization model**
 - Most of the existence models use very simplistic assumptions.
 - How does the co-polar ratio vary in different environments?
 - How can we compare existence measurement based models in a strictly same sense? **Advanced statistical analysis is necessary.**

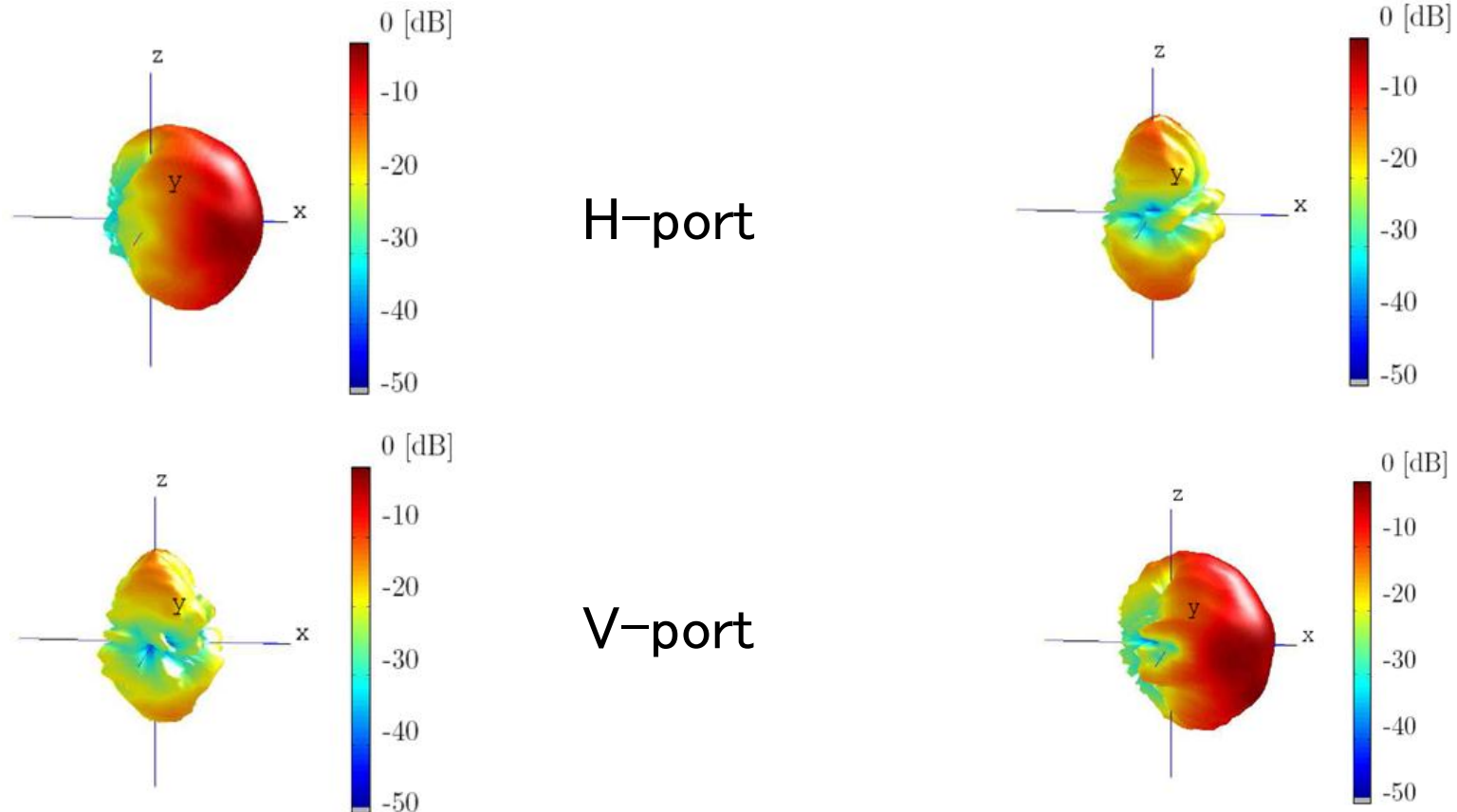
Polarization: Theory and Practice

- Polarization: time variations of electric field
 - Depolarization
 - by Rain
 - by Ionosphere (Faraday rotation)
 - by scattering: most significant cause for MIMO



Polarization: in Practice

- Horizontal excitation
- Vertical excitation

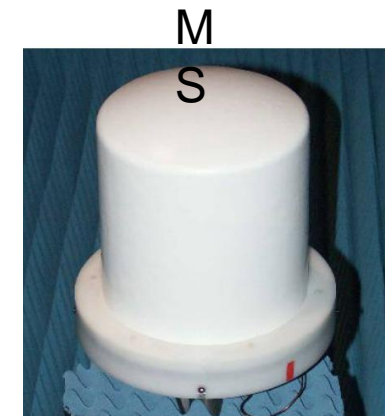


Power “Leak” exists. **➡** Measurement based model

Channel sounding system

RUSK channel sounder

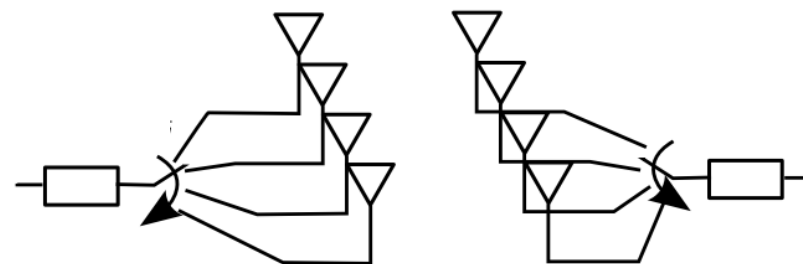
Carrier freq.	4.5 GHz
Bandwidth	120 MHz
BS antenna (V-H pol.)	Uniform Rectangular Array $2 \times 4 \times 2$ pol. Elements
MS antenna (V-H pol.)	Stacked Uniform Circular Array $2 \times 24 \times 2$ pol. elements
Transmit signal	Wideband multitone
Max. delay	$3.2 \mu\text{s}$
No. of MIMO channels	1536



- Fully switched system
- Rubidium reference clocks for switching frame synchronization



Double-directional measurement



Parameter estimation

- RIMAX:

Gradient-based maximum likelihood parameter estimation

- Including diffuse scattering components
- Based on the conjugate gradient optimization strategy
- Variance of estimated parameter is used to improve model reliability

- RIMAX outputs:

$\gamma_{VV}, \gamma_{VH}, \gamma_{HV}, \gamma_{HH}$	Complex polarimetric path weights
θ^{BS}, ϕ^{BS}	Elevation and Azimuth angle at BS
θ^{MS}, ϕ^{MS}	Elevation and Azimuth angle at MS
τ	Delay

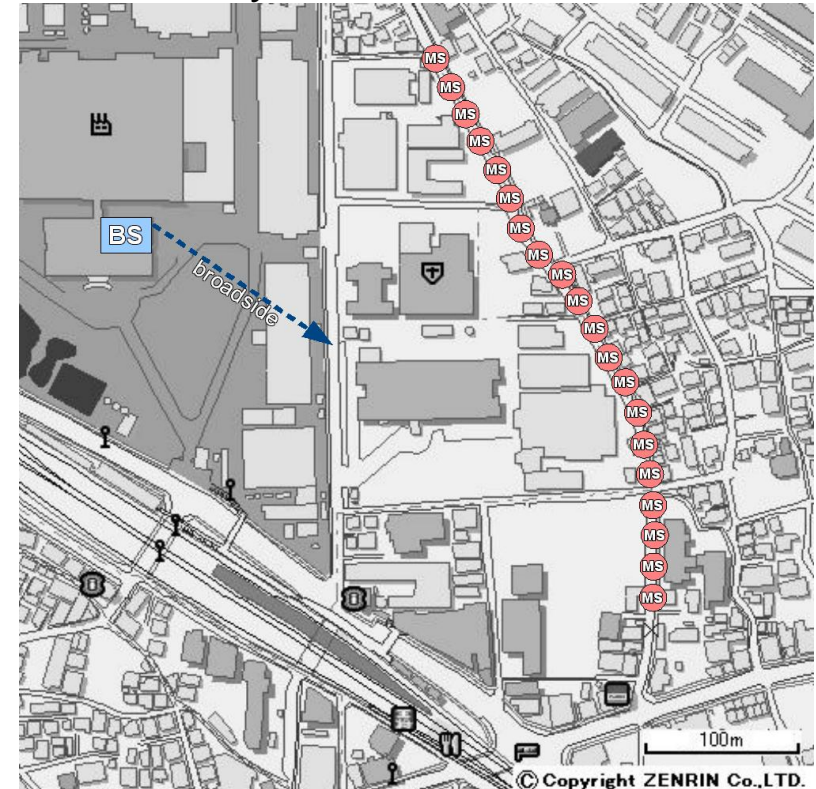
Environment

- BS : highest in the area
- MS interval: 20 m (along the street)
- 6 snapshots are taken every MS position (50-60 snapshots measured)

Small Macrocell Scenario

BS height	85 m
MS height	1.80 m
BS-MS distance	230m ~ 400 m
MS status	Static; moving (slow walk)
Structure type	Residential & industrial

Layout of the scenario.



Kawasaki City, Japan

Multipath clusterization

- Cluster:
 - set of paths experienced similar propagation mechanism
 - * Cluster-wise modeling approach was adopted as COST273 framework
- Automatic multipath clusterization
 - Second treatment of measured data
 - Details can be found in [1] and [2]
- Notes for the data treatment
 - 6 snapshots for every MS position were averaged.
 - Dynamic parameters are not considered.
 - Strongest paths (corresponds to the LoS) were removed using single path estimation.

[1] L. Materum et al., Proc. Int. Symp. Antennas Propag. (ISAP), pp. 854-857, Oct. 2008.

[2] L. Materum et al., EURASIP J. Wireless Commun. and Netw., Feb.2009.

Polarization Ratio

- XPR: degree of depolarization from being V polarized to being H polarized, or vice versa.

$$\text{XPR}_V^{\text{BS}} = 10 \log_{10} \left(\frac{\sum_{l \in \mathcal{C}_k} |\gamma_{VV,l}|^2}{\sum_{l \in \mathcal{C}_k} |\gamma_{VH,l}|^2} \right)$$

$$\text{XPR}_V^{\text{MS}} = 10 \log_{10} \left(\frac{\sum_{l \in \mathcal{C}_k} |\gamma_{VV,l}|^2}{\sum_{l \in \mathcal{C}_k} |\gamma_{HV,l}|^2} \right)$$

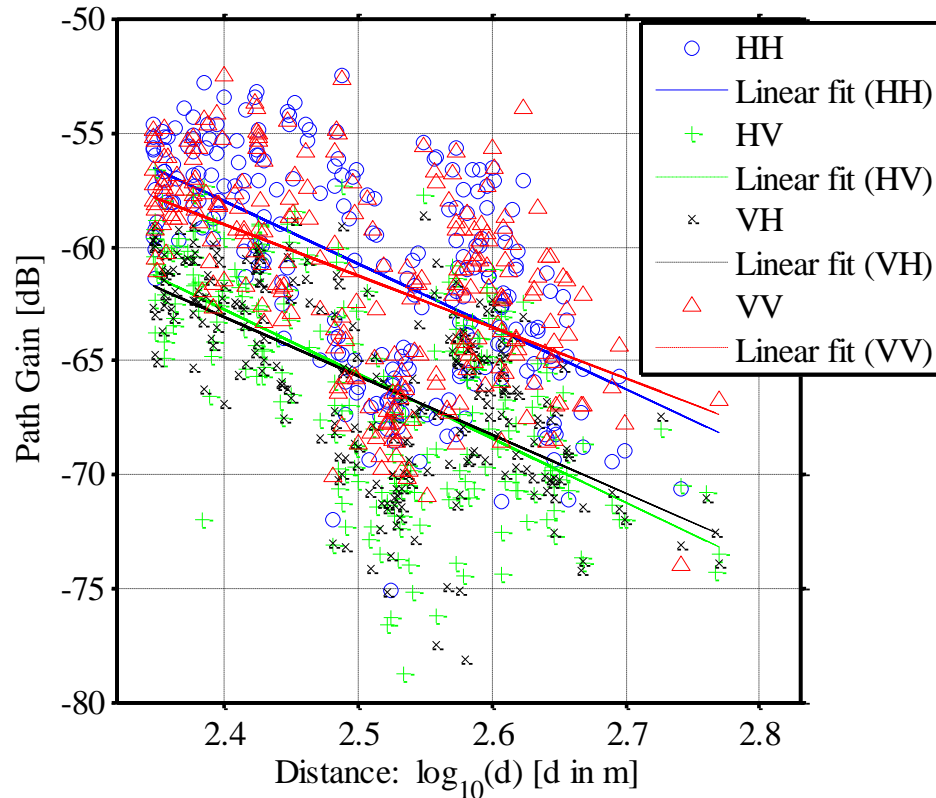
$$\text{XPR}_H^{\text{BS}} = 10 \log_{10} \left(\frac{\sum_{l \in \mathcal{C}_k} |\gamma_{HH,l}|^2}{\sum_{l \in \mathcal{C}_k} |\gamma_{HV,l}|^2} \right)$$

$$\text{XPR}_H^{\text{MS}} = 10 \log_{10} \left(\frac{\sum_{l \in \mathcal{C}_k} |\gamma_{HH,l}|^2}{\sum_{l \in \mathcal{C}_k} |\gamma_{VH,l}|^2} \right)$$

- CPR: degree of V polarization with respect to the H polarization.

$$\text{CPR} = 10 \log_{10} \left(\frac{\sum_{l \in \mathcal{C}_k} |\gamma_{VV,l}|^2}{\sum_{l \in \mathcal{C}_k} |\gamma_{HH,l}|^2} \right)$$

Polarization Path Gain



$$P_{HH} = -27.57 \log_{10}(d) + 8.21$$

$$P_{HV} = -28.28 \log_{10}(d) + 5.12$$

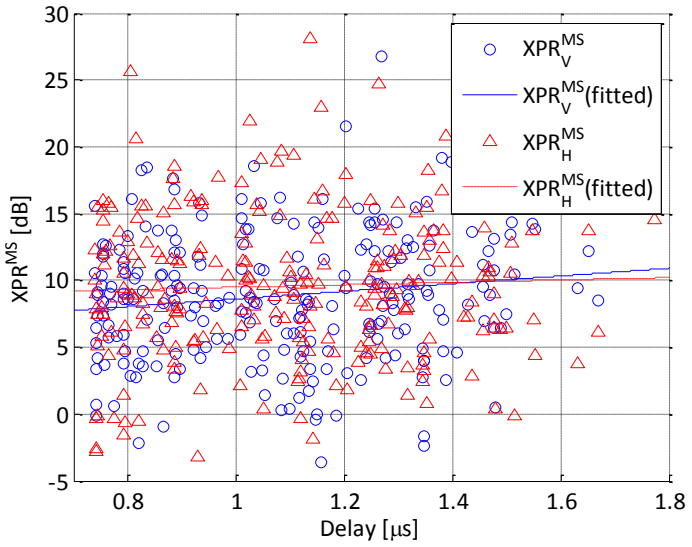
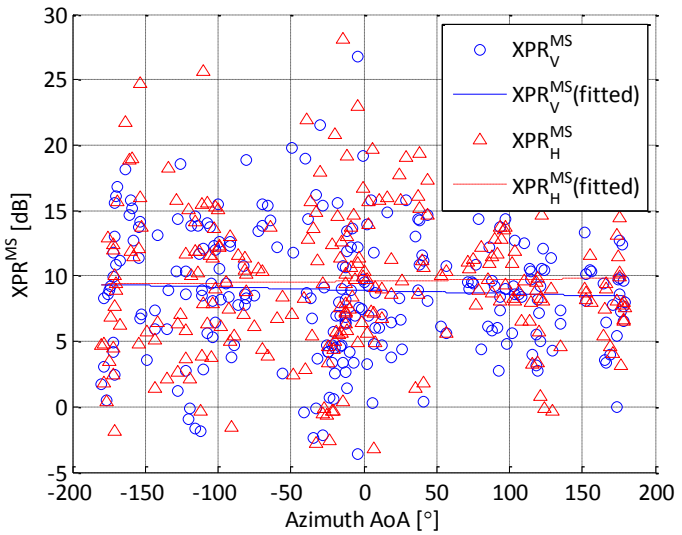
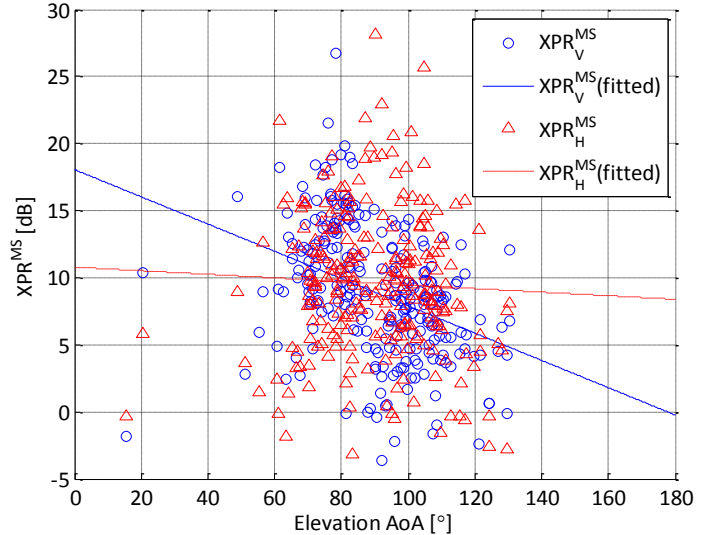
$$P_{VH} = -25.81 \log_{10}(d) - 1.14$$

$$P_{VV} = -22.55 \log_{10}(d) - 4.88$$

Decay coefficient			
HH	VV	HV	VH
-27.58	-24.55	-28.28	-25.81

- HH polarization pairs decay faster than VV polarization pairs.
- Co-pol. path gains were **4.65dB** higher than the cross-pol. ones.
- Similar observations;
 - [5], [6] : HH decays faster than VV.
 - [3] : co-pol. is 4~10dB higher than cross-pol.
 - [4] : co-pol. is 7dB higher than cross-pol.

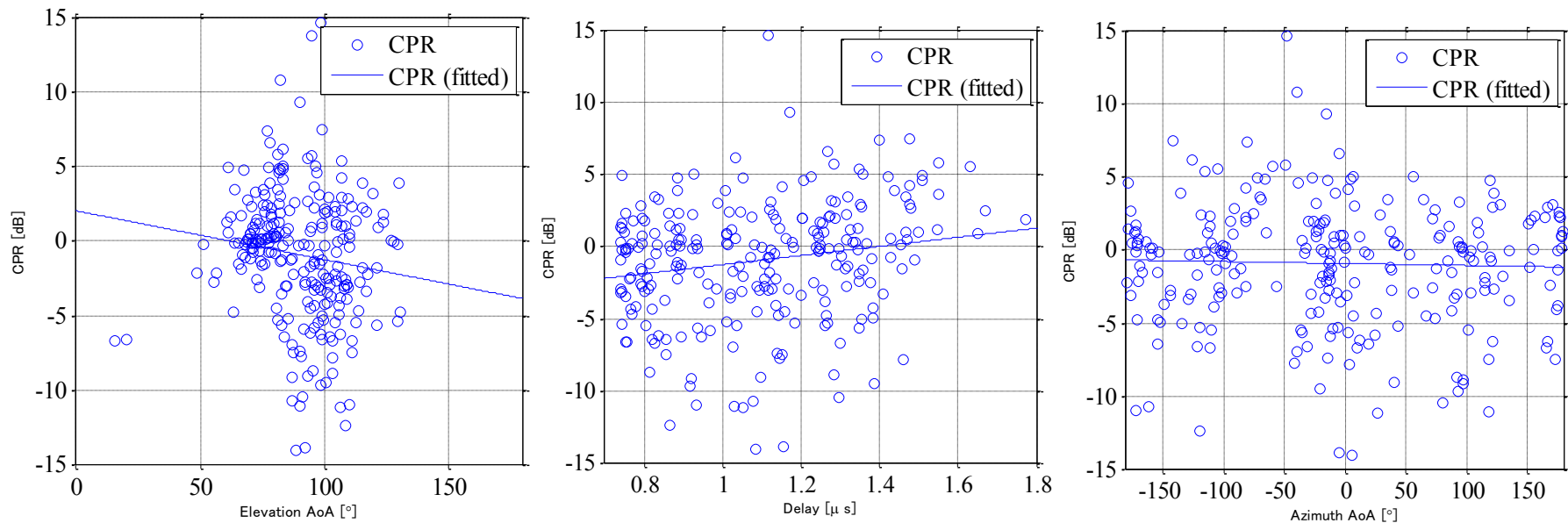
XPR characteristics



Decay coefficient

XPR vs.	V pol.	H pol.
Elevation AoA	-0.12	-0.03
Azimuth AoA	-0.003	0.001
Delay	2.97	0.96

CPR characteristics



Decay coefficient

	CPR
Elevation AoA	-0.0327
Azimuth AoA	-0.0013
Delay	3.1714

Comparison of Decay coefficient
dose not clarify the polarization behavior

Dependency quantification

- Correlation coefficient:

- Linear-Linear: Delay and Elevation

$$-1 \leq \frac{\text{Cov}(x, y)}{\sqrt{\text{Var}(x) \times \text{Var}(y)}} \leq 1$$

- Linear-Circular: Azimuth

$$R_{x\theta}^2 = \frac{r_{xc}^2 + r_{xs}^2 - 2r_{xc}r_{xs}r_{cs}}{1 - r_{cs}^2}$$

$$r_{xc} = \text{corr}(x, \cos(\theta))$$

$$r_{xs} = \text{corr}(x, \sin(\theta))$$

$$r_{cs} = \text{corr}(\cos(\theta), \sin(\theta))$$

Medium correlation is observed between XPR_V^{MS} and elevation AoA

Variable x	Variable y		
	Elevation	Azimuth	Delay
XPR_V^{MS}	-0.3705	0.0013	0.1535
XPR_H^{MS}	-0.0437	0.0079	0.0433
CPR	-0.1354	0.0005	0.1926

Summary of Previous Work

Achievement

- Polarization behavior is analyzed by Regression approach
- Only the rough characteristics were studied

Problem

- The correlation coefficient indicates only the ordinal relation
- Difficult to compare with other results

Solution

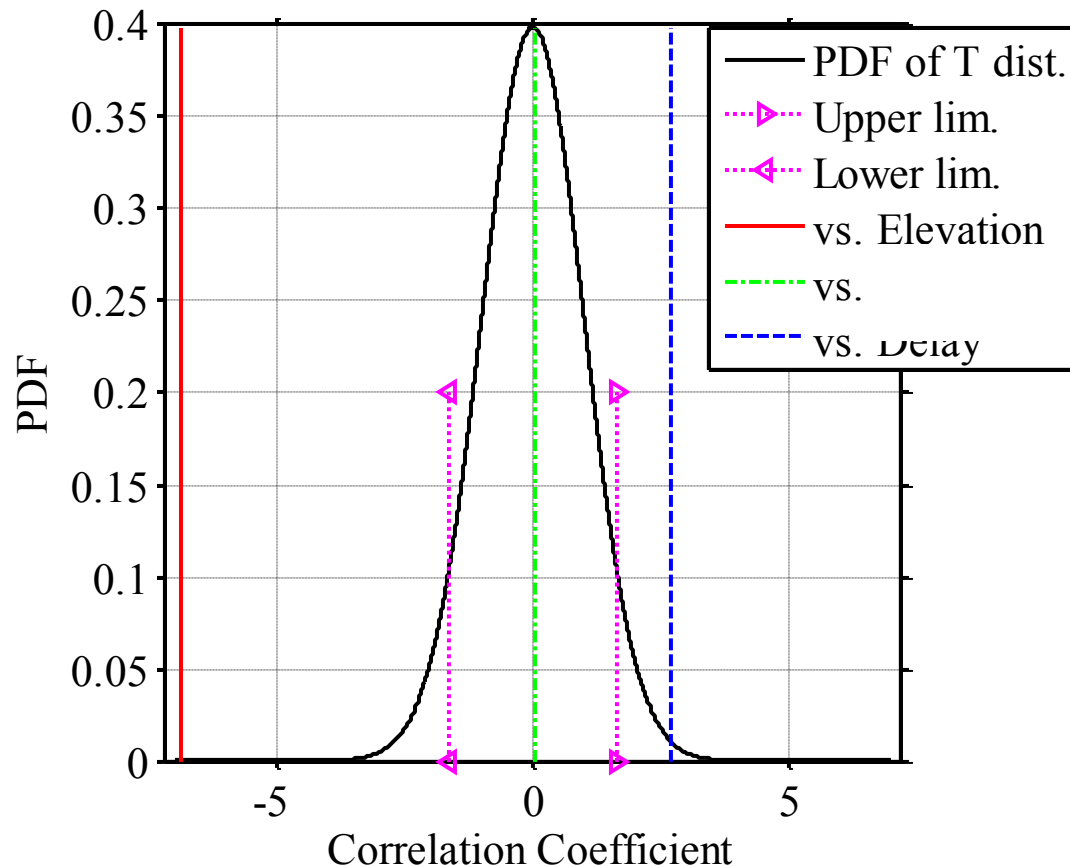
- Strictly statistical analysis: Hypothesis testing

Procedure of Hypothesis Testing: T-Test

- Step 1
 - Assume “total correlation coefficient” = 0 (null hypothesis)
- Step 2
 - Compute the test statistics:
$$t = \frac{\bar{x} - \mu}{\sqrt{\sigma^2/n}}$$
- Step 3
 - Plot the probability density of T distribution with
Significance level = 0.05
Degree of freedom = 251 (Sample size)
- Step 4
 - Judgment: in the PDF plot,
 - I. 5% < “total correlation coefficient” < 95%
XPR/CPR is **independent on** the parameter in 5 % significance level
 - II. 5% > “total correlation coefficient” & “total correlation coefficient” > 95 %
XPR/CPR is **dependent on** the parameter in 5 % significance level

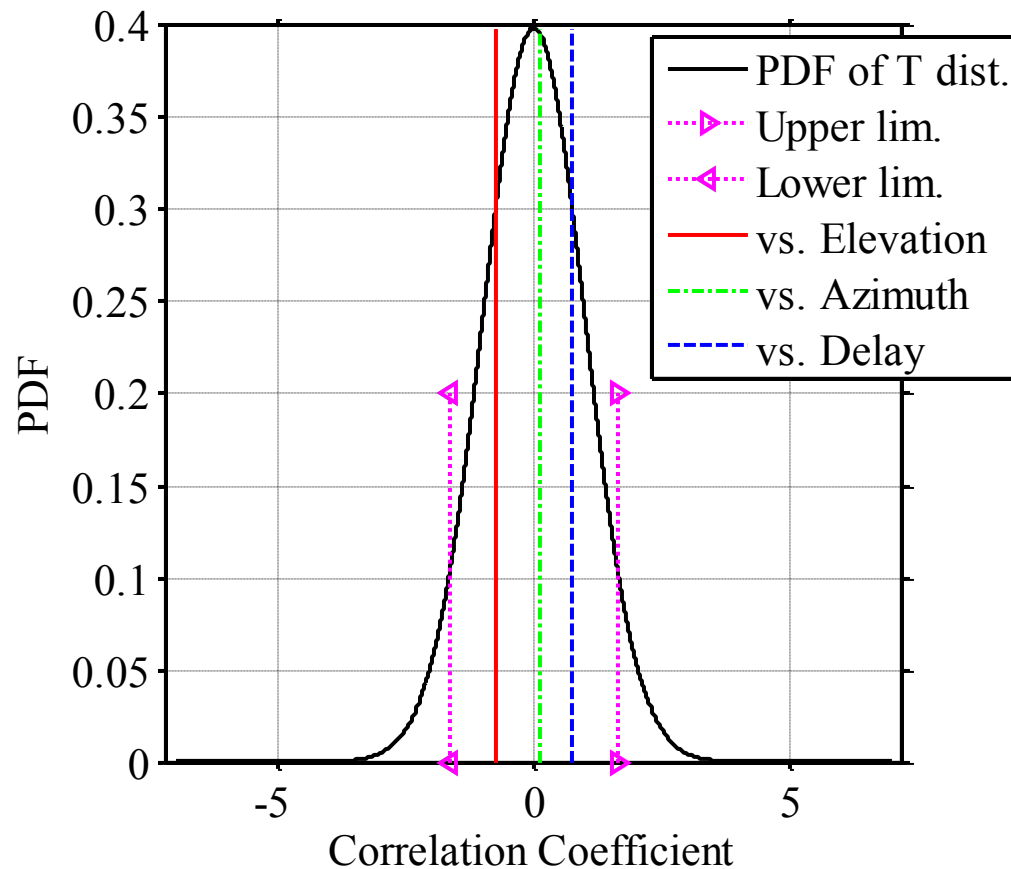
V polarization: XPR at MS

- V pol. : independent with Azimuth and Delay
: dependent on Elevation



H polarization: XPR at MS

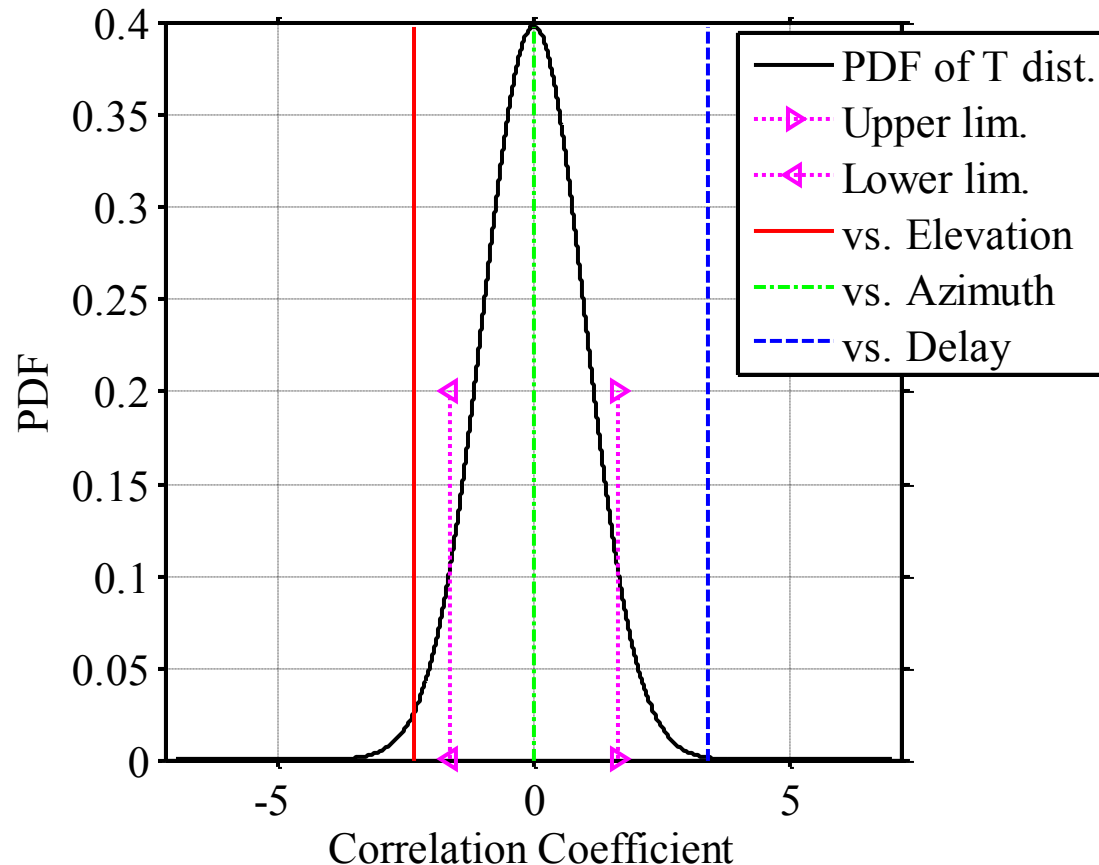
- H pol. : independent with all parameters



CPR results

- CPR : independent with Delay

: dependent on Azimuth and Elevation



Conclusions

- Multipath cluster polarization characteristics of a small urban macrocell at 4.5 GHz has been presented
- XPR and CPR dependency on the parameters were analyzed and validated by hypothesis testing

Future works

- Comparison by presented approach
 - Different measurement sites
 - Different parameter estimation algorithms
 - RIMAX outputs (path-wise)
 - Clustering outputs
 - Beamforming outputs
 - >Need more study to analyze polarization behavior
- Planning of the new measurement campaign
 - Proper scenario selection
 - Clear objective setting: focus on polarization

References

- [1] L. Materum, J. Takada, I. Ida, and Y. Oishi, "Improved multipath clustering of a small urban macrocellular MIMO environment at 4.5 GHz," Proc. Int. Symp. Antennas Propag. (ISAP), pp. 854-857, Oct. 2008.
- [2] L. Materum, J. Takada, I. Ida, and Y. Oishi, "Mobile station spatio-temporal multipath clustering of an estimated wideband MIMO double-directional channel of a small urban 4.5 GHz macrocell," EURASIP J. Wireless Commun. and Netw., Feb. 2009.
- [3] R. Vaughan, "Polarization diversity in mobile communications," IEEE Trans. Veh. Technol., vol. 39, pp. 177-186, Aug. 1990.
- [4] L. M. Correia (Ed.), Mobile Broadband Multimedia Networks (Techniques, Models and Tools for 4G), Elsevier, 2006.
- [5] I. Sirkova, "Overview of COST 273 Part I: propagation modeling and channel characterization", XLI ICEST, Sofia, Bulgaria, 2006.
- [6] I. Sirkova, "Overview of COST 273 Part II: Parabolic equation method application", XLI ICEST, Sofia, Bulgaria, 2006.
- [7] <http://www.cost2100.org/>
- [8] BY P. E. JUPP, AND K. V. MARDIA, "A general correlation coefficient for directional data and related regression problems," Biometrika, 67, 1, pp. 163-73, 1980

Thank you for listening!
